

## The Electron Temperatures of H II Regions Determined from Radio Recombination Line Observations at 22 GHz

T. L. Wilson, J. Bieging, and W. E. Wilson

Max-Planck-Institut für Radioastronomie, Auf dem Hügel 69, D-5300 Bonn, Federal Republic of Germany

Received November 21, 1977; revised May 8, 1978

**Summary.** This paper presents radial velocities, line widths and LTE electron temperatures obtained from the H 66 $\alpha$  line together with continuum measurements for 15 strong H II regions measured at 22.4 GHz with a resolution of  $\sim 43''$ . The ratio of the intensities of the H 83 $\beta$  to the H 66 $\alpha$  lines, measured for 5 sources, is consistent with LTE. Hence the effect of stimulated emission is small, and the true and LTE electron temperatures are directly related. The average LTE electron temperature for the sources in the survey is 7900 K. Our LTE electron temperatures are in excellent agreement with the H 66 $\alpha$  data for six sources measured by Waltman and Johnston (1973) with an angular resolution of 2.3'. We conclude that there are no large gradients in the electron temperature for these sources and the effects of source geometry (Lockman and Brown (1976)) are also small at 22.4 GHz. We compare these data with the H 109 $\alpha$  and H 137 $\beta$  data of Churchwell et al. (1977), measured with a 2.6' resolution. The agreement between the H 109 $\alpha$  and H 66 $\alpha$  electron temperatures (calculated assuming Local Thermodynamic Equilibrium) is surprisingly good, whereas the LTE electron temperatures calculated from the H 137 $\beta$  line are, on the average,  $1800 \pm 600$  K higher than the LTE electron temperatures obtained from the H 66 $\alpha$  line data. Any theoretical explanations of these results can be tested only for Orion A, for which the most data are available. The new H 66 $\alpha$  and H 109 $\alpha$  data require a modification of the Brocklehurst and Seaton model (1972), in which substantial clumping must be included. Our results are not extensive enough to fully test the proposed gradient in electron temperatures of H II regions with distance from the galactic center but the H 66 $\alpha$  data are consistent with such a gradient.

**Key words:** recombination lines — LTE electron temperatures — H II regions

The observations of radio recombination lines at frequencies higher than 20 GHz are valuable because: (1) the continuum optical depth of the sources is low, so that the recombination line emission is not affected by stimulated emission and the true electron temperatures of H II regions can be calculated accurately; (2) the telescope beam size is smaller than at lower frequencies, so that structure in H II regions can be resolved; (3) at high frequencies, the dense cores of compact H II regions, such as W 3 (OH) are optically thin, so the properties of high density ionized gas can be investigated and (4) the effect of Stark broadening of recombination lines will be negligible. As emphasized by Brown et al. (1978) the electron temperatures obtained from recombination lines measured at high frequencies will refer to the densest parts of the H II regions. Previous surveys of the radio recombination lines of hydrogen at frequencies above 20 GHz, made by Berulis et al. (1975) and Waltman and Johnston (1973), had angular resolutions of 2–3'. These groups reported electron temperatures (calculated assuming Local Thermodynamic Equilibrium, hereafter LTE) of 7000–8000 K, considerably lower than the generally accepted value of  $10^4$  K. The motivation for the present survey was: (1) to reduce the uncertainties in the LTE electron temperatures measured previously by taking advantage of the large collecting area of the 100 m telescope, and (2) to use the  $\sim 43''$  beam of the telescope to investigate conditions in the compact cores of H II regions.

### Observations

The observations were made with the 100 m telescope of the Max-Planck Institut für Radioastronomie in November 1976. At 22.364 GHz, the rest frequency of the H 66 $\alpha$  line, the full width to half power of the telescope beam is  $\sim 43''$ . The aperture and beam efficiencies of the telescope are a fairly strong function of elevation at this frequency. In the zenith the aperture efficiency is 0.3 and the beam efficiency is 0.4, for the inner 80 m of the telescope. The receiver was a cooled parametric

---

*Send offprint requests to:* T. L. Wilson

**Table 1.** Continuum and H 66 $\alpha$  line data

(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
Source Name	Source coordinates		Observed Source Size	$\theta_\alpha$	Source Flux Density	Velocity	Full Width to Half Power	Line to Continuum Ratio	Electron Temperature		Distance from Galactic Center
	R.A. (1950)	Decl. (1950)	$\theta_\alpha$	$\theta_\delta$	$S_\nu$	$V_{LSR}$	$\Delta V_{1/2}$	$T_L/T_c$ a)	LTE $T_e$	Model $T_e$ b)	$R_{GC}$
	h m s	o ' "	(")	(")	(Jy)	(km s $^{-1}$ )	(km s $^{-1}$ )		(K)	(K)	(kpc)
W3 A	02 21 57	+61 52 41	54	60	30	-39.1 $\pm$ 0.2	27.7 $\pm$ 1.6	0.23 $\pm$ 0.02 (2)	8400 $\pm$ 1200	8700	12
W3 B	02 21 50	+61 52 34	--	51	--	-39.5 $\pm$ 0.2	26.0 $\pm$ 1.0	0.24 $\pm$ 0.04 (3)	8500 $\pm$ 1300	9000	12
Orion A	05 32 47	-05 25 23	136	195	375	-1.4 $\pm$ 0.6	25.8 $\pm$ 0.5	0.25 $\pm$ 0.01 (2)	8200 $\pm$ 300	8500	10.5
Orion A (1.6'S)	05 32 50	-05 26 49	--	--	--	-2.2 $\pm$ 0.2	26.2 $\pm$ 0.4	0.26 $\pm$ 0.01 (1)	7700 $\pm$ 500	----	10.5
NGC 2024	05 39 13	-01 56 15	156	84	36	6.4 $\pm$ 0.2	22.4 $\pm$ 0.5	0.34 $\pm$ 0.01 (1)	7200 $\pm$ 500	6800	10.5
Mon R2	06 05 19	-06 22 29	45	45	8	12.1 $\pm$ 0.5	27.6 $\pm$ 1.4	0.21 $\pm$ 0.01 (1)	9000 $\pm$ 800	9300	$\sim$ 11
Sgr B2	17 44 10	-28 22 12	48	$\sim$ 54	24	61.7 $\pm$ 0.4	35.0 $\pm$ 1.2	0.21 $\pm$ 0.01 (1)	7500 $\pm$ 500	8500	0.2
W33	18 11 18	-17 56 32	43	43	27	36.2 $\pm$ 0.2	32.3 $\pm$ 0.5	0.28 $\pm$ 0.01 (1)	6100 $\pm$ 300	6900	5
M17	18 17 33	-16 13 23	93	183	216	15.4 $\pm$ 0.3	31.4 $\pm$ 0.7	0.21 $\pm$ 0.01 (1)	8000 $\pm$ 300	8200	8
W49 (5)	19 07 50	+09 01 29	70	48	24	6.3 $\pm$ 0.1	27.9 $\pm$ 0.4	0.25 $\pm$ 0.02 (1)	7700 $\pm$ 600	7900	9.5
W49 (6)	19 07 58	+09 00 18	42	51	8	10.6 $\pm$ 0.3	34.0 $\pm$ 0.8	0.20 $\pm$ 0.01 (1)	7800 $\pm$ 500	8200	9.5
W51 B	19 21 15	+14 24 13	60	60	13	66.2 $\pm$ 0.6	27.1 $\pm$ 0.7	0.23 $\pm$ 0.03 (1)	8500 $\pm$ 800	8000	8
W51 D	19 21 22	+14 25 19	81	57	36	56.4 $\pm$ 0.1	31.0 $\pm$ 0.6	0.26 $\pm$ 0.01 (2)	6800 $\pm$ 300	6800	8
W51 E	19 21 24	+14 24 52	54	66	55	58.0 $\pm$ 0.2	29.5 $\pm$ 0.4	0.24 $\pm$ 0.02 (2)	7400 $\pm$ 800	8200	8
K3-50	19 59 58	+32 25 53	43	43	3	-16.5 $\pm$ 0.6	32.2 $\pm$ 1.7	0.21 $\pm$ 0.02 (1)	8000 $\pm$ 600	8400	10
DR 21	20 37 14	+42 08 55	45	45	21	-0.7 $\pm$ 0.3	32.7 $\pm$ 3.0	0.19 $\pm$ 0.02 (2)	8400 $\pm$ 500	9500	10

a) in parentheses are the number of independent observations included in the determination of  $T_e$

b) corrections to the LTE electron temperatures were made assuming that the H II regions are uniform density, isothermal spheres, using the line and continuum data in Table 1 and the  $b_n$  and  $\beta$  values of Brocklehurst (1970). We emphasize that the model  $T_e$ 's are based only on the 22 GHz data. The model electron temperatures are related to the LTE electron temperatures by Eq. (3), which is solved iteratively

amplifier which typically had a noise temperature of 160 K, referred to the feed horn. Atmospheric attenuation increased the system noise by between 40 K and 150 K, depending on weather conditions and source elevation. The spectrometer was a 384-channel autocorrelator with a 10 MHz bandwidth, giving a spectral resolution of 31.5 kHz ( $=0.4$  km s $^{-1}$ ). Spectral line measurements were made by switching between positions separated by 5" of time in Right Ascension, with on-source and off-source integration times of 5 min, so that the source and reference spectra covered the same range of azimuth and elevation.

Continuum measurements were made by scanning across the source in both right ascension and declination. The receiver was stabilized against gain drifts by load switching, except in the case of K 3-50 and DR 21. These two sources are small enough to permit beam switching (the separation of the beams is 112"), which provided excellent cancellation of baseline variations caused by the weather. For the other, more extended sources, the principal source of uncertainty in the measured continuum intensities is the fluctuation in the zero level because of the weather.

Since the main purpose of these observations was to determine the ratio of the integrated line intensity to the continuum intensity, the continuum and line measurements were made at nearly equal elevations. In general, a source was first scanned to measure the continuum intensity; then the spectrum was obtained in

one or more pairs of 5" integrations. If the source moved through a significant range of elevation angles during the spectral integration, a continuum scan was repeated at the end of the spectral measurement and the adopted continuum intensity was taken as a mean value. This procedure was used for both the H 66 $\alpha$  and the H 83 $\beta$  line measurements. For our determination of the H 83 $\beta$ /H 66 $\alpha$  ratio the effects of weather, telescope elevation, etc., were eliminated by requiring that the continuum temperatures measured in conjunction with the H 66 $\alpha$  or H 83 $\beta$  lines are equal, and adjusting the line temperatures accordingly.

## Results

### H 66 $\alpha$ Line

The basic observational data for the sources are summarized in Table 1. The source sizes,  $\theta_\alpha$  and  $\theta_\delta$ , are the widths at half-maximum intensity measured by hand from the continuum scans, and have not been corrected for broadening by the  $\sim 43''$  telescope beam. The uncertainties in the source sizes are  $\sim 5''$ . The flux density was determined from the peak intensity (corrected for elevation) and the measured size. The flux density scale was determined by scans across either NGC 7027 or W 3 (OH), which were assumed to have a flux densities of 6.0 Jy or 3.5 Jy at 22.4 GHz respectively. The uncertainties in the flux densities are estimated to be 30%.

**Table 2.** H 83 $\beta$  line results

(1)	(2)	(3)	(4)
Source Name	$V_{\text{LSR}}$ (km s <sup>-1</sup> )	$\Delta V_{1/2}$ (km s <sup>-1</sup> )	$\frac{T_L(\text{H}83\beta)}{T_L(\text{H}66\alpha)} \frac{\Delta V_{1/2}(\text{H}83\beta)}{\Delta V_{1/2}(\text{H}66\alpha)}$
W3 A	-37.5 $\pm$ 0.4	30.2 $\pm$ 1.2	0.23 $\pm$ 0.03
W3 B	-40.0 $\pm$ 0.5	27.5 $\pm$ 1.3	0.26 $\pm$ 0.03
Orion A	+ 0.4 $\pm$ 0.6	25.5 $\pm$ 0.4	0.27 $\pm$ 0.02
NGC 2024	+ 6.3 $\pm$ 1.0	25.6 $\pm$ 0.6	0.32 $\pm$ 0.05
W51 E	+57.5 $\pm$ 0.2	31.3 $\pm$ 0.7	0.30 $\pm$ 0.01

<sup>a)</sup> The LTE value of the  $\beta$  to  $\alpha$  ratio is 0.276

The intensity, center velocity  $V$  (relative to the LSR) and the full width to half power of the H 66 $\alpha$  line were determined for each source by a gaussian fit to the spectrum. The results were compared with visual estimates of these parameters from the plotted spectra. The agreement was generally very good, except in a few cases where the spectral baseline was curved. The uncertainties quoted in Table 1 reflect both the formal errors of the gaussian fit and the degree of consistency between fitted and directly measured values. Because, as discussed earlier, the measured line and continuum intensities are functions of source elevation, we do not give in Table 1 a value for the peak line temperature alone. Instead we give the ratio of the line to continuum antenna temperature, which is the relevant parameter for calculating an electron temperature. We define  $R$  as

$$R = \frac{T_L}{T_c} \cdot \Delta V_{1/2}, \quad (1)$$

where  $(T_L/T_c)$ , the line-to-continuum ratio, is given in Col. 9 of Table 1. The full width to half power  $\Delta V_{1/2}$ , is given in Col. 8 of Table 1. The LTE electron temperature of the H II region,  $T_e^*$ , which produces the observed H 66 $\alpha$  emission is given by

$$T_e^* = \frac{1.84 \cdot 10^5 (N^+/N_e)}{R \left\{ \frac{3}{2} \log T_e^* - 2.66 \right\}} = \frac{1.84 \cdot 10^5 (N^+/N_e)}{R g(T_e^*)}. \quad (2)$$

Eq. (2) must be solved iteratively.  $g(T_e^*)$  is the Gaunt factor.  $(N^+/N_e)$  is the ratio of proton density to electron density. Except for NGC 2024, we have taken the ratio of singly ionized helium to hydrogen to be 0.08. Then  $(N^+/N_e)$  is  $(1.08)^{-1}$ . For NGC 2024, where the ionized helium to ionized hydrogen ratio is 0.03 [Churchwell et al. (1977)], we have used  $(1.03)^{-1}$ . Values of  $T_e^*$ , the LTE electron temperature, are listed in Col. 10 of Table 1. The quoted uncertainties reflect primarily the uncertainty of the continuum temperature, since the error in the line data is small. Finally, the distance of the H II region from the center of the galaxy is given in Col. 12. Distances are based in most cases on kinematic determinations using the measured radial velocities. Distance estimates for sources with large non-circular

**Table 3.** Comparison of electron temperatures derived from H 66 $\alpha$  and H 56 $\alpha$  observations

Source	LTE Electron Temperature, $T_e^*$		
	(H56 $\alpha$ ) (Berulis et al.)	(H66 $\alpha$ ) (Waltman & Johnston)	(H66 $\alpha$ ) (This paper)
W3	8260 $\pm$ 600	8100 $\pm$ 1700	8400 $\pm$ 1200 <sup>a)</sup>
Orion A	7670 $\pm$ 500	7800 $\pm$ 800	8200 $\pm$ 300
NGC 2024	8400 $\pm$ 650	7000 $\pm$ 1300	7200 $\pm$ 500
Sgr B2	-- --	-- --	7500 $\pm$ 500
M17	-- --	7150 $\pm$ 800	8000 $\pm$ 300
W49	-- --	7150 $\pm$ 1300	7800 $\pm$ 600 <sup>a)</sup>
W51	6960 $\pm$ 500	7450 $\pm$ 1000	7300 $\pm$ 500 <sup>a)</sup>
DR21	7020 $\pm$ 700	-- --	8400 $\pm$ 500

<sup>a)</sup> Average electron temperature, weighted by the continuum temperatures of the components in the region

velocities, such as Sgr B 2 and W 33 are discussed in notes and comments on the individual sources, which are given in the Appendix.

### H 83 $\beta$ Line

For five sources, the H 83 $\beta$  line was also observed in the same manner as the H 66 $\alpha$  line. The ratio of the integrated intensities of these two lines furnishes a measure of the departure from LTE in the ionized gas. The results are summarized in Table 2. The derived center velocities and line widths agree to within 1 or 2 $\sigma$  with the corresponding values for the H 66 $\alpha$  line from Table 1. The value of the  $\beta$ - to  $\alpha$ -intensity under LTE conditions is 0.28. The values for this ratio in Col. 4 are consistent with the LTE value to within 1 $\sigma$  for W 3 B, Orion A, and NGC 2024, and to within 2 $\sigma$  for W 3 A and W 51 E. These data indicate that, at least in these sources, the recombination lines at 22 GHz are formed very nearly under conditions of thermodynamic equilibrium.

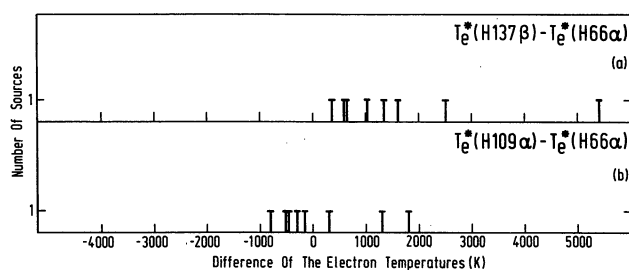
### Corrections for Stimulated Emission

Although the H 66 $\alpha$  lines are very nearly formed in LTE, one can estimate the true electron temperature,  $T_e$ , using corrections for non-LTE effects, from

$$T_e = b_n T_e^* \{ (g(T_e^*)/g(T_e)) \} (1 + \frac{1}{2} (1 - \beta) \tau_c), \quad (3)$$

where  $b_n$  is the departure coefficient,  $\beta$  is the stimulated emission term,  $\tau_c$  is the continuum optical depth at the line frequency, and  $g$  is the Gaunt factor. Eq. (3) must be solved iteratively because the values of  $b_n$  and  $\beta$  depend on the true electron temperature and electron density. We have estimated these source parameters from the model calculation computer program of Walmsley and Churchwell. The model is based on:

- (1) The assumption that the H II region is isothermal,



**Fig. 1.** **a** The distribution of the difference between the H 137 $\beta$  and H 66 $\alpha$  LTE Electron Temperatures. The source at the extreme right, with a difference of 5400 K, is Sgr B 2, and the source with a difference of 2500 K is DR 21. **b** A histogram of the difference between the H 109 $\alpha$  and H 66 $\alpha$  LTE Electron Temperatures. The source which has a difference of 1900 K is Sgr B 2, and the source with a difference of 1300 K is DR 21.

has a uniform density and is spherical, and (2) the line and continuum parameters in Table 1 (we have used the source sizes given in Col. (4) and (5) after correcting for the telescope beam assuming gaussian source and beam shapes), and (3) the  $b_n$  and  $\beta$  values of Brocklehurst (1970).

The angular sizes of W 3 B, W 33, W 49(6) and K 3–50 are considerably smaller than our beam and we have used sizes obtained from aperture synthesis maps. The references from which these sizes were obtained are listed in the Appendix. The LTE electron temperature at the position 1.6' south of the peak of Orion A was not corrected. The amount of the correction depends on the geometry, for example, Pauls and Wilson (1977) assumed that Orion A had a gaussian source shape and found that no correction for stimulated emission was required at 22 GHz, in contrast to the 4% correction given in Table 1. We conclude that geometry can affect non-LTE corrections by 5%. The corrections for stimulated emission are less than 13% for the sources we have observed, and we will use the LTE electron temperatures in the following discussions.

## Discussion

### Comparisons with Other Observations of High Frequency Recombination Lines

In Table 3 we compare our values for  $T_e^*$  with those surveys made at high frequencies which include more than 1 source, and where the errors in  $T_e^*$  are less than 20%. Berulis et al. (1975) give  $T_e^*$  results for the H 56 $\alpha$  line (rest frequency=36.46 GHz), and Waltman and Johnston list  $T_e^*$  values for the H 66 $\alpha$  line. On the average our values of  $T_e^*$  are slightly larger than those obtained in either of the other two surveys. However, with the exception of the  $T_e^*$  value for DR 21, the results agree at the  $1\sigma$  level. Considering the difference in beamsize (the other surveys had telescope beams  $\geq 2'$ ), the agreement is very good. The agreement with the survey of Waltman and Johnston (made with a resolu-

**Table 4.**

(1)	(2)	(3)	(4)	(5)	(6)	(7)
Source	H83 $\alpha$ /H66 $\alpha$ Ratio	H137 $\beta$ /H109 $\alpha$ Ratio	$T_e^*$ (H66 $\alpha$ ) (This paper)	$T_e^*$ (H109 $\alpha$ ) (Churchwell et al.)	$T_e^*$ (H137 $\beta$ ) (Churchwell et al.)	$T_e$ (Model) <sup>d)</sup>
W3	0.24 $\pm$ 0.02 <sup>a)</sup>	0.20 $\pm$ 0.01	8400 $\pm$ 1200	7920	10000	10910
Orion A	0.27 $\pm$ 0.02	0.23 $\pm$ 0.003	8200 $\pm$ 300	8050	9240	11170
NGC 2024	0.32 $\pm$ 0.01	0.30 $\pm$ 0.01	7200 $\pm$ 500	7510	7560	8810
Sgr B2		0.19 $\pm$ 0.01	7500 $\pm$ 500	9300	12900	13620
M17		0.21 $\pm$ 0.005	8000 $\pm$ 300	7550	9060	11380
W49		0.20 $\pm$ 0.006	7800 $\pm$ 600 <sup>c)</sup>	7480	9150	10420
W51	0.30 $\pm$ 0.01 <sup>b)</sup>	0.22 $\pm$ 0.007	7300 $\pm$ 500	6530	7970	9310
DR21		0.24 $\pm$ 0.02	8400 $\pm$ 500	9790	10920	16690

<sup>a)</sup> Unweighted average for W 3 A and W 3 B.

<sup>b)</sup> Result for W 51 E only.

<sup>c)</sup> Average electron temperature, weighted by source continuum of components in region.

<sup>d)</sup> These model  $T_e$ 's are based only on 5 GHz data.

tion of 2.3'), makes it unlikely that systematic spatial gradients in the electron temperatures in H II regions and the effects of source geometry [emphasized by Lockman and Brown (1976)] are present for these sources at 22.4 GHz.

### Comparison of $T_e^*$ Values from H 137 $\beta$ , H 109 $\alpha$ , and H 66 $\alpha$ Data

We compare  $T_e^*$  values from the H 137 $\beta$  and H 109 $\alpha$  line survey of Churchwell et al. (1977) with our results in Table 4. A plot of the difference between the H 66 $\alpha$   $T_e^*$  and the  $T_e^*$ 's from the H 137 $\beta$  and H 109 $\alpha$  data are given in Figs. 1a and 1b. The average value of the  $T_e^*$  from the H 109 $\alpha$  line is 200 K larger than the average  $T_e^*$  from the H 66 $\alpha$  line. This difference is smaller than the  $1\sigma$  errors in either set of data. On the other hand, the  $T_e^*$  from the H 137 $\beta$  line data is 1800 K larger than the  $T_e^*$  from the H 66 $\alpha$  line. This difference is more than twice the standard error of the mean, 600 K.

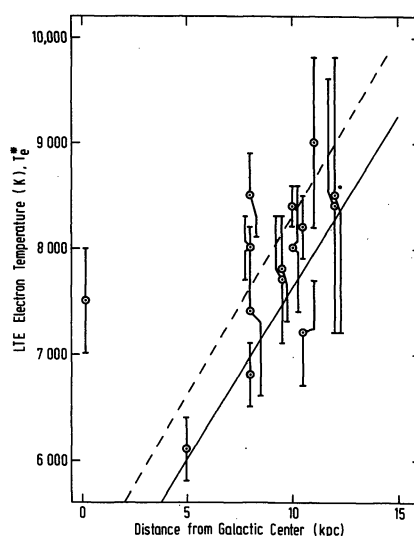
The two sources with the largest differences in the LTE electron temperatures at 5 and 22 GHz, both for the H 137 $\beta$  and H 109 $\alpha$  lines, are Sgr B 2 and DR 21. Continuum optical depth effects must play a large role. Excluding these two H II regions, the LTE electron temperatures obtained from the H 137 $\beta$  data are  $1000 \pm 200$  K (uncertainty is the error of the mean) larger than the LTE electron temperatures obtained from the H 66 $\alpha$  line data. Although the 2.6' resolution of the H 137 $\beta$  and H 109 $\alpha$  data is 15 times the area of the  $\sim 43''$  beam used to take the H 66 $\alpha$  results, we have previously argued that large temperature gradients are not present at 22 GHz, and hence one can compare these data. For the sources in Table 4, the average width of the H 66 $\alpha$  line is  $\sim 3$  km s $^{-1}$  smaller than the average width of the H 109 $\alpha$  line. Such a difference can be



explained by the large difference in the angular resolution in these surveys, and mass motions in the H II regions. However the average of the widths of the H 137 $\beta$  lines of the sources in Table 4 is  $\sim 4 \text{ km s}^{-1}$  larger than the average of the widths of the H 109 $\alpha$  lines. Since these data were taken with the same resolution at the same frequency, mass motions of the ionized gas cannot account for the difference. As pointed out by Churchwell et al., pressure broadening is probably the cause.

The ratio of the H 137 $\beta$  to H 109 $\alpha$  line should be 0.276 if both lines are formed in LTE. Except for NGC 2024, these values, given in Table 4, show that the ratio is more than  $3\sigma$  below the LTE value and non-LTE effects are present. The usual interpretation has been that the H 109 $\alpha$  lines more strongly stimulated than the H 137 $\beta$  lines and that the  $T_e^*$  values obtained from the H 137 $\beta$  lines are closer to the true electron temperature. Although Lockman and Brown (1976) have pointed out that geometrical effects might affect these  $\beta$  to  $\alpha$  ratios for a spherical H II region with variable density and electron temperature, the unpublished data of Churchwell et al. show no such effects in Orion A, and in the following we will assume that a plane-parallel geometry accurately represents the source structure.

The most surprising result of the comparison is the agreement of the  $T_e^*$ 's from the H 66 $\alpha$  and H 109 $\alpha$  data, because the H 66 $\alpha$  emission is weighted toward dense gas which is close to LTE, while the H 109 $\alpha$  emission is weighted towards more diffuse ionized gas which is affected by stimulated emission. A detailed investigation of a possible causal relationship between the  $T_e^*$ 's values can be carried out only for Orion A, where we have enough data. From the H 66 $\alpha$  (Pauls and Wilson, 1977), and H 109 $\alpha$  (Churchwell et al.) data there are no large temperature gradients in this source. Hence the true electron temperature of the H 109 $\alpha$  line formation region is  $\sim 7000$ – $8000 \text{ K}$ . However, to have  $T_e^*$  equal the true electron temperature, stimulated emission, which lowers  $T_e^*$  must be balanced by pressure broadening. Pressure broadening shifts some of the line intensity into broad, weak wings, which are on the order of the noise. These wide wings are lost in the baseline fits and hence the  $T_e^*$  is raised. Both effects, stimulated emission and pressure broadening may be on the order of 10–20% of the line intensity, and it seems that the agreement of  $T_e^*$  (H 66 $\alpha$ ) and  $T_e^*$  (H 109 $\alpha$ ) is caused by the fact that both effects are the same size. To obtain the necessary amount of collisional broadening, the true electron density must be more than twice the r.m.s. electron density. Hence the clumping factor, which is the square of ratio of the electron densities, is more than 4, and only 25% of the nebula is filled with ionized gas of density  $> 10^4 \text{ cm}^{-3}$ . The large clumping factor is in agreement with estimates obtained from optical observations.



**Fig. 2.** The H 66 $\alpha$  LTE Electron Temperatures obtained from our H 66 $\alpha$  line data plotted against distance from the galactic center. The average LTE Electron Temperature, weighted inversely by the square of the error is 7900 K. The two sources located within 5 kpc of the galactic center are W 33 and Sgr B 2. For these sources the true electron temperature may be significantly different from  $T_e^*$ , either because of stimulated emission or because of optical depth effects. The dotted line gives the average value of the LTE Electron Temperature obtained by Churchwell et al. from their 137 $\beta$  line data, and the solid line is the corresponding Electron Temperature obtained from the H 109 $\alpha$  line data

### Radial Gradients in $T_e^*$ in the Galaxy

Fig. 2 shows our  $T_e^*$  plotted as a function of distance from the galactic center. We also show the gradient in  $T_e^*$  obtained by Churchwell et al. for the H 109 $\alpha$  and H 137 $\beta$   $T_e^*$ 's. Our data do not cover a large enough range in distance from the galactic center to test the H 109 $\alpha$  results of Churchwell et al., but the H 66 $\alpha$  results are consistent with the gradient in LTE electron temperature with distance from the galactic center given by Churchwell et al.

**Acknowledgement.** We thank P. Shaver and especially C. M. Walmsley for helpful criticism. E. Churchwell and C. M. Walmsley kindly provided unpublished data and also the computer program used to calculate the model electron temperatures.

### Appendix

#### Notes to Table 1

W 3A and W 3B. These are the two strongest sources in the continuum complex W 3. These sources are barely separated by our beam. W 3A has a shell structure and W 3B has a gaussian-like shape. On the basis of an H 109 $\alpha$  aperture synthesis map, Wellington et al. (1976) had claimed that the radial velocities of W 3A and B were significantly different. Our H 66 $\alpha$  velocities, however, are equal to within the uncertainties. For the corrections to the electron temperature (col. 12, Table 1), we took the angular size of W 3B, 17'', from Wynn-Williams (1971).

Orion A and Ori A (1.6'S). These are the two prominent peaks in the Orion H II region. The region around the peak of Orion A has been mapped by Pauls and Wilson (1977). The second peak, 1.6' south of the main source, is a newly detected object and its nature is unknown. This second peak is present in the interferometer map of Martin and Gull (1976), but is not prominent on optical photographs.

NGC 2024. The flux density of this source is considerably lower than 55 Jy, the flux density obtained by integrating maps of the source (Schraml and Mezger, 1969; Shaver and Goss, 1970). The difference in the flux density is caused by our low values of the angular size. Because the source has at least two components, our parameters may refer only to the denser one.

Mon R 2. Our angular size and flux density is consistent with the value given by Downes et al. (1975). The lower limit to the central emission measure at 10.7 GHz given by Downes et al.,  $7.4 \times 10^6 \text{ cm}^{-6} \text{ pc}$ , would cause 7% stimulated emission at 22 GHz. However it is possible that the source is somewhat optically thick at 10.7 GHz, and even higher emission measure components are present.

Sgr B 2. Our data refer to one set of components in this complex, that referred to as sources 3 and 5 by Martin and Downes (1972). A second component called source 4 by Martin and Downes, 1' north of this source, has a radial velocity of  $70.8 \pm 0.8 \text{ km s}^{-1}$ . The rapid change indicates that large velocity gradients are present in the H II region. We did not include the second component in Table 1 because of uncertainties in the continuum data. Our flux density is about 10 times that reported by Martin and Downes, but our flux estimates undoubtedly include a large contribution from the smooth background, not present in the interferometer map. We follow Reifenstein et al. (1970) in assuming that the Sgr B 2 complex is 200 pc from the galactic center.

W 33. This is the dense component in the H II region complex. We have used the distance to the source presented by Gardner et al. (1975), and the angular size of  $\sim 14'' \times \sim 27''$ , given by Goss et al. (1977). Our flux density agrees well with the 10.7 GHz value of Goss et al.

M 17. Our data refer only to the southern peak in this source, hence our flux densities and angular sizes, etc. do not represent values for the entire nebula. The flux density of the entire nebula is 609 Jy (Schraml and Mezger, 1969).

W 49. Our data refer to the dense components 5 and 6 of Wynn-Williams (1971). The size for component 6 used in the calculation of the source optical depth, was taken from Wynn-Williams (1971). The trend in the radial velocities, i.e. increasing radial velocity with increasing Right Ascension, is in agreement with the lower-resolution results of Gordon and Wallace (1971).

W 51. The source numbering was taken from the interferometer map of W 51 by Martin (1972). Radial velocities measured with an angular resolution of 4' showed that this, the northern part of the W 51 complex, had velocities below  $60 \text{ km s}^{-1}$ , while the group of sources 24' SW had radial velocities above  $68 \text{ km s}^{-1}$ . Using this information, Wilson et al. (1970) has proposed that the W 51 region consists of two independent groups of sources, at 7 and 8.5 kpc from the Sun. Component B, for which the H 66 $\alpha$  line velocity is  $66.2 \text{ km s}^{-1}$ , is located in the group which exhibited velocities of  $58 \text{ km s}^{-1}$  in the data of Wilson et al. This might indicate that peculiar velocities in this region are  $\sim 12 \text{ km s}^{-1}$ , and the simple model of Wilson et al. should be revised. The flux densities reported by Martin (1972) for component B agree to within 30% of our value. However, our flux densities for components D and E exceed Martin's by factors of 3 and 1.5, respectively. As Martin points out, these sources are optically thick between 2.7 and 5 GHz, where he obtained the flux density data, but a larger contribution may come from a smooth background which is resolved by the interferometer.

K 3-50. Our data refer to the northernmost compact component in this complex. This component is referred to as K 3-50 C, and is resolved into two components with a 2'' resolution (Harris, 1975). Our flux density agrees with the 5 GHz value of Harris (1975), and we have used the average of the angular sizes of the components listed by Harris in our computation of the corrected electron temperature. Unpublished H 90 $\alpha$  data of Wilson and Jaffe made with a resolution of 90'', do not show the H 66 $\alpha$  velocity, but rather a range of radial velocities between  $-29$  and  $-23 \text{ km s}^{-1}$ . However K 3-50 C is compact and dilution in the 90'' beam would be significant. This component is located within 10'' of the 1720 MHz OH maser center in K 3-50, and the radial velocity of the H 66 $\alpha$  line is within  $3 \text{ km s}^{-1}$  of the velocity of the OH line.

DR 21. Our data probably refer to the components A, B, and C in the interferometer map of Harris (1973). Our value of the LTE electron temperature,  $T_e^*$ , agrees very well with the  $T_e^*$  obtained from an analysis of the radio continuum flux densities measured at various frequencies (see e.g. Salem and Seaton, 1974). Although our flux density agrees very well with that reported at lower frequencies by Harris (1975), the line width,  $43 \text{ km s}^{-1}$ , and radial velocity,  $-2.5 \text{ km s}^{-1}$ , of the recombination lines measured at 5 GHz (Churchwell et al.) differ from our values by much more than the quoted errors. Hence the 5 GHz recombination lines may be formed in a completely different region.

## References

- Brocklehurst, M.: 1970, *Monthly Notices Roy. Astron. Soc.* **148**, 417  
 Brocklehurst, M., Seaton, M. J.: 1972, *Monthly Notices Roy. Astron. Soc.* **157**, 179  
 Berulis, I. I., Smirnov, G. T., Sorochenko, R. L.: 1975, *Soviet Astron. Letters* **1**, 187  
 Brown, R. L., Lockman, F. J., Knapp, G. R.: 1979, *Ann. Rev. Astron. Astrophys.* (in press)  
 Churchwell, E., Smith, L. F., Mathis, J., Mezger, P. G., Huchtmeier, W.: 1979, *Astron. Astrophys.* **70**, 719  
 Downes, D., Winnberg, A., Goss, W. M., Johansson, E. B.: 1975, *Astron. Astrophys.* **44**, 243  
 Gardner, F. F., Wilson, T. L., Thomasson, P.: 1975, *Astrophys. Letters* **16**, 29  
 Gordon, M. A., Wallace, D.: 1971, *Astrophys. J.* **167**, 235  
 Goss, W. M., Matthews, H. E., Winnberg, A.: 1978, *Astron. Astrophys.* **65**, 307  
 Harris, S.: 1973, *Monthly Notices Roy. Astron. Soc.* **162**, 5p  
 Harris, S.: 1975, *Monthly Notices Roy. Astron. Soc.* **170**, 139  
 Lockman, F. J., Brown, R. L.: 1976, *Astrophys. J.* **207**, 436  
 Martin, A. H. M.: 1972, *Monthly Notices Roy. Astron. Soc.* **157**, 31  
 Martin, A. H. M., Downes, D.: 1972, *Astrophys. Letters* **11**, 219  
 Martin, A. H. M., Gull, S. F.: 1976 *Monthly Notices Roy. Astron. Soc.* **179**, 217  
 Pauls, T., Wilson, T. L.: 1977, *Astron. Astrophys.* **60**, L31  
 Reifenstein, E. C. III, Wilson, T. L., Burke, B. F., Mezger, P. G., Altenhoff, W. J.: 1970, *Astron. Astrophys.* **4**, 357  
 Salem, M., Seaton, M. J.: 1974, *Monthly Notices Roy. Astron. Soc.* **167**, 493  
 Schraml, J., Mezger, P. G.: 1969, *Astrophys. J.* **156**, 269  
 Shaver, P. A., Goss, W. M.: 1970, *Australian J. Phys. Astrophys. Suppl.* **14**, 133  
 Waltman, E. B., Johnston, K. J.: 1973, *Astrophys. J.* **182**, 489  
 Wellington, K. J., Sullivan, W. T. III, Goss, W. M., Matthews, H. E.: 1976, *Astron. Astrophys.* **47**, 351  
 Wilson, T. L., Mezger, P. G., Gardner, F. F., Milne, D. K.: 1970, *Astrophys. Letters* **5**, 99  
 Wynn-Williams, C. G.: 1971, *Monthly Notices Roy. Astron. Soc.* **151**, 397